

### Core Geometry Coefficient For Resonant Inductors\*

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A resonant inductor is required to have a small size, a low power loss, and good heat dissipation. In particular, it is difficult to design an optimal inductor for high-frequency and high-power applications. The design methods for resonant inductors presented until now are based on the trial-and-error approach. There is no criterion to pick the candidates for the core for resonant inductors from different core-product companies.

The core geometry coefficient ( $K_g$ ) is one of the useful criteria to select the core [1]-[5]. By using the  $K_g$  method, it is possible to select the core satisfying the acceptable wire loss, the electromagnetic conditions, and a core area restriction. However, there are no considerations and examples of the design procedure of resonant inductors using the  $K_g$  method.

This paper presents expressions of the core geometry coefficient for the resonant inductor design. Additionally, a design example of a resonant inductor for a class-E power amplifier is given. By using the proposed expressions, the core geometry coefficient is determined from the electrical specifications of the loaded quality factor of a series-resonant circuit, the output power, the operating frequency, the maximum flux density, and the maximum wire loss. It is a good criterion to select the core from different manufacturers.

#### Basic Theory And Derivation Of Core Geometry Coefficient $K_g$

The inductance of an inductor with an air gap is given by

$$L = \frac{N^2}{\frac{l_g}{\mu_0 A_c} + \frac{l_c}{\mu_r \mu_c A_c}} = \frac{\mu_0 N^2 A_c}{l_g + \frac{l_c}{\mu_r}}, \quad (1)$$

where  $N$  is the number of wire turns,  $l_g$  is the air-gap length,  $l_c$  is the core length,  $A_c$  is the cross-sectional area of the magnetic core,  $\mu_0$  is the free-space permeability, and  $\mu_r$  is the relative permeability of a core material.

In general, it can be written that

$$Ni = B \left( \frac{l_g}{\mu_0} + \frac{l_c}{\mu_0 \mu_r} \right), \quad (2)$$

where  $B$  is the magnetic flux density. Hence,

$$B_m = \frac{\mu_0 N I_m}{\frac{l_c}{\mu_r} + l_g}, \quad (3)$$

where  $B_m$  and  $I_m$  are the maximum flux density and the maximum inductor current. From (1) and (3), the number of turns is

$$N = \frac{LI_m}{A_c B_m}, \quad (4)$$

which is a requirement from electromagnetic point of view. The length of the winding wire is

$$l_w = Nl_T, \quad (5)$$

where  $l_T$  is the mean length of a single turn (MLT). The dc winding resistance is

$$R_{wdc} = \frac{\rho_w l_w}{A_w} = \frac{\rho_w N l_T}{A_w}, \quad (6)$$

where  $A_w$  and  $\rho_w$  are the cross-sectional area of the winding bare wire and the resistivity of the copper, respectively. Therefore,

$$A_w = \frac{N \rho_w l_T}{R_{wdc}}. \quad (7)$$

The dc and low-frequency wire loss is

$$P_{wdc} = R_{wdc} I_{rms}^2, \quad (8)$$

where  $I_{rms}$  is the root-mean-square value of the inductor current. Therefore, (7) is rewritten as

$$A_w = \frac{N \rho_w l_T I_{rms}^2}{P_{wdc}}. \quad (9)$$

The core window utilization factor is defined as the ratio of the cross-sectional area of the winding bare wire  $A_{Cu}$  to the window cross-sectional area of a core  $W_a$

$$K_u = \frac{A_{Cu}}{W_a} = \frac{N A_w}{W_a}. \quad (10)$$

From (9) and (10), we obtain

$$N^2 = \frac{K_u W_a P_{wdc}}{\rho_w l_T I_{rms}^2} \quad (11)$$

and

$$A_w^2 = \frac{K_u W_a \rho_w l_T I_{rm}^2}{P_{wdc}} \quad (12)$$

These relations include both the wire-loss condition in (9) and the core-area condition in (10). The number of turns should also satisfy the electromagnetic condition in (4). Equating the right-hand sides of (4) and (11), the *core geometry coefficient* [1] is obtained as

$$K_g = \frac{W_a A_c^2 K_u}{l_T} = \frac{\rho_w L^2 I_m^2 I_{rms}^2}{P_{wdc} B_m^2} = \frac{2\rho_w L W_m I_{rms}^2}{P_{wdc} B_m^2} \quad (\text{m}^5), \quad (13)$$

where the maximum energy stored in the inductor is

$$W_m = \frac{L I_m^2}{2} \quad (14)$$

It is convenient to express the dc wire loss as the ratio of the output power  $P_{wdc} = \alpha P_o$ , resulting in

$$K_g = \frac{\rho_w L^2 I_m^2 I_{rms}^2}{\alpha P_o B_m^2} = \frac{2\rho_w L W_m I_{rms}^2}{\alpha P_o B_m^2} \quad (15)$$

The core geometry coefficient  $K_g$  provides the core with a good combination of  $W_a$ ,  $A_c$ , and  $l_T$  satisfying the electromagnetic condition in (7), the dc-wire-loss condition in (9), and the core-area restriction in (10) simultaneously. In [2],  $K_g$  of many cores at  $K_u = 0.4$  is presented or can be calculated from the core dimensions.

### Core Geometry Coefficient For Resonant Inductors

We consider the design of resonant inductors conducting a sinusoidal current  $i_L = I_m \sin \omega t$ , where  $\omega = 2\pi f$  is the angular frequency and  $I_m = \sqrt{2} I_{rms}$  is the amplitude of the sinusoidal current. From (15), we obtain

$$K_g = \frac{\rho_w L^2 I_m^4}{2\alpha P_o B_m^2} = \frac{2\rho_w W_m^2}{\alpha P_o B_m^2} \quad (16)$$

Generally, the loaded quality factor of a series-resonant **L – C – R** circuit is defined as

$$Q_L = \frac{\omega L}{R} = \frac{\omega L I_m^2}{2P_o} = \frac{\omega W_m}{P_o} \quad (17)$$

Thus, the core geometry coefficient for resonant inductors is given by

$$K_g = \frac{2\rho_w Q_L^2 P_o}{\alpha \omega^2 B_m^2} \quad (18)$$

By using the proposed expressions for  $K_g$  in (16) and (18), we can select the core satisfying the conditions (7), (9), and (10), using only the electrical parameters.

### Design Example

This paper presents a design example of a resonant inductor for the class E resonant power amplifier [7], whose topology is shown in Fig. 1. We design the resonant inductor  $L$  to meet the following specifications:  $f = 100$  kHz,  $P_o = 80$  W,  $R_L = 70 \Omega$ , and  $Q_L = 5$ . From these specifications, we obtain  $I_m = \sqrt{2P_o/R_L} = 1.51$  A, and  $L = QR/\omega = 557 \mu\text{H}$ . The inductor specifications are:  $J_m < 5$  A/mm<sup>2</sup>,  $K_u = 0.4$ , and  $B_m = 0.2$  T, where  $J_m$  is the maximum current density of the wire. Design examples of the dc-feed inductor  $L_c$  are given in [5].

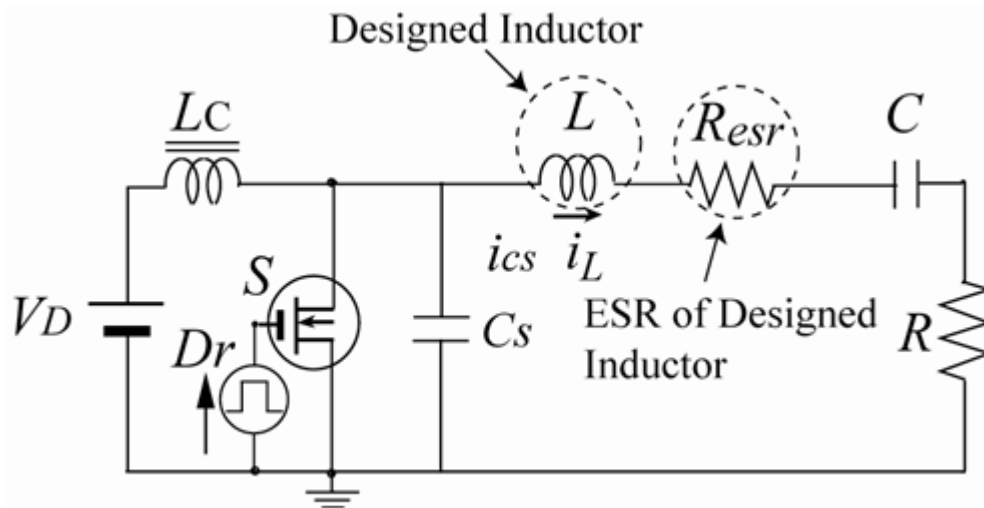


Fig. 1. Class-E power amplifier.

### Wire Loss, Core Loss, And Current Density

In the first design example, we allow 0.5% of the output power to be the wire loss in the inductor, that is,  $\alpha = 0.005$ . From (18), the core geometry coefficient increases with the decrease in the wire loss, which usually implies a large core volume. Therefore, the core loss increases with the decrease of the wire loss. The core loss is large in resonant inductors because of a high frequency and a large value of  $I_m$ . Therefore, the selection of the value of  $\alpha$  is crucial in the design of the resonant inductors.

From (18), the core geometry coefficient is obtained as

$$\begin{aligned} K_g &= \frac{2\rho_w Q_L^2 P_o}{\alpha \omega^2 B_m^2} \\ &= \frac{2 \times 1.72 \times 10^{-7} \times 5^2 \times 80}{0.005 \times 2 \times \pi \times 100 \times 10^3 \times 0.2^2} \\ &= 8.73 \times 10^{-13} (\text{m}^5) = 0.00873 \text{ cm}^5. \end{aligned} \quad (19)$$

We select NEC/TOKIN FEE-30W core with the following parameters [2], [8]:  $K_g = 0.0100 \text{ cm}^5$ ,  $A_c = 0.412 \text{ cm}^2$ ,  $W_c = 1.36 \text{ cm}^2$ ,  $l_T = 5.1 \text{ cm}$ ,  $l_c = 4.7 \text{ cm}$ ,  $V_c = 1934 \text{ mm}^3$ . From (12), the bare wire cross-sectional area is given by

$$\begin{aligned}
 A_w &= \sqrt{\frac{K_u W_a \rho_w l_T I_m^2}{2 \alpha P_o}} \\
 &= \sqrt{0.4 \times 1.36 \times 10^{-4} \times 1.72 \times 10^{-8}} \\
 &\quad \times \sqrt{5.1 \times 10^{-2} \times 1.51^2} \\
 &\quad / \sqrt{2 \times 0.005 \times 80} \quad (\text{m}^2) \\
 &= 0.275 \text{ mm}^2.
 \end{aligned} \tag{20}$$

The maximum current density of the wire is

$$\begin{aligned}
 J_m &= \frac{I_m}{A_w} = \frac{1.51}{0.275 \times 10^{-6}} \quad (\text{A/m}^2) \\
 &= 5.49 \text{ A/mm}^2 > 5 \text{ A/mm}^2.
 \end{aligned} \tag{21}$$

Since the current density is higher than that given by the regulation, the NEC/TOKIN FEI-25 core cannot be used for this inductor. The current-density restriction is rarely not satisfied and can be neglected for the design of inductors used in dc-dc converters in CCM and DCM [1]. This result indicates that the current density is one of the bottle-neck for the design of resonant inductors and we should carefully consider the current density restriction. For a low current density, a thick wire is required as shown in (20). A thicker wire yields a lower wire loss and smaller  $\alpha$ , which provides a higher  $K_g$  value as shown in (18).

### Inductor Design

We reset  $\alpha = 0.0025$  and obtain

$$\begin{aligned}
 K_g &= \frac{2 \rho_w Q_L^2 P_o}{\alpha \omega^2 B_m^2} \\
 &= \frac{2 \times 1.72 \times 10^{-7} \times 5^2 \times 80}{0.0025 \times 2 \times \pi \times 100 \times 10^3 \times 0.2^2} \\
 &= 1.75 \times 10^{-12} (\text{m}^5) = 0.0175 \text{ cm}^5.
 \end{aligned} \tag{22}$$

We reselect NEC/Tokin FEE-25W core with the following parameters [2], [8]:  $K_g = 0.0204 \text{ cm}^5$ ,  $A_c = 0.417 \text{ cm}^2$ ,  $W_c = 1.49 \text{ cm}^2$ ,  $l_T = 5.1 \text{ cm}$ ,  $l_c = 7.2 \text{ cm}$ ,  $V_c = 3010 \text{ mm}^3$ . The core dimensions  $C, D, E$  and  $F$ , defined in Fig. 2, are  $C = 7 \text{ mm}$ ,  $D = 12.2 \text{ mm}$ ,  $E = 25.3 \text{ mm}$ , and  $F = 6.8 \text{ mm}$ .

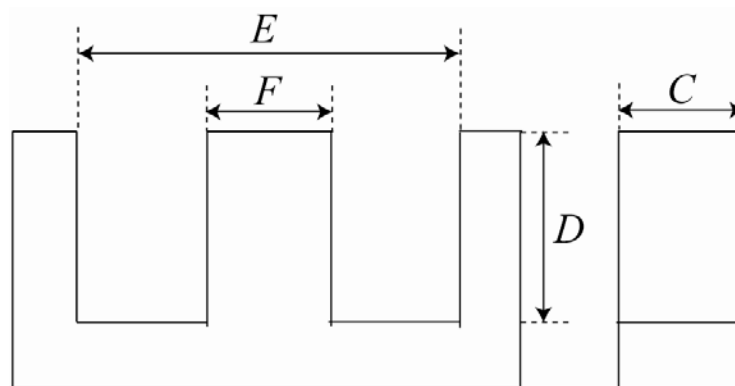


Fig.2 Mechanical parameters of E core.

Additionally, BH1 core material is chosen with  $\mu_r = 2300 \pm 20\%$  and  $P_v = 400 \text{ kW/m}^3$  for  $f = 100 \text{ kHz}$  and  $B_m = 0.2 \text{ T}$ , where  $P_v$  is the core power loss per unit volume. Following the same procedure as that in (20) and (21), we can obtain

$$\begin{aligned}
 A_w &= \sqrt{\frac{K_u W_a \rho_w l_T I_m^2}{2\alpha P_o}} \\
 &= \sqrt{0.4 \times 1.49 \times 10^{-4} \times 1.72 \times 10^{-8}} \\
 &\quad \times \sqrt{7.2 \times 10^{-2} \times 1.51^2} \\
 &\quad / \sqrt{2 \times 0.0025 \times 80} \quad (\text{m}^2) \\
 &= 0.542 \text{ mm}^2
 \end{aligned} \tag{23}$$

and

$$\begin{aligned}
 J_m &= \frac{I_m}{A_w} = \frac{1.51}{0.542 \times 10^{-6}} \quad (\text{A/m}^2) \\
 &= 2.77 \text{ A/mm}^2 < 5 \text{ A/mm}^2.
 \end{aligned} \tag{24}$$

This core satisfies the current-density restriction.

**Single-Strand Winding.** From the calculated cross-sectional area  $A_w = 0.542 \text{ mm}^2$  in (20), an AWG 19 copper wire with  $A_w = 0.653 \text{ mm}^2$  and a bare wire diameter  $d = 0.912 \text{ mm}$  is selected. Because the nominal outer diameter of the AWG 19 wire is  $d_o = 0.98 \text{ mm}$ , the number of turns is obtained from

$$\begin{aligned}
 N &= \frac{K_u W_a}{A_w} \\
 &= \frac{0.4 \times 1.49 \times 10^{-4}}{0.653 \times 10^{-6}} = 91.2 \text{ turns}.
 \end{aligned} \tag{25}$$

We pick  $N = 91$  turns. For the adjustment of the inductance  $L$ , the air-gap length is calculated as

$$\begin{aligned}
 l_g &= \frac{\mu_0 A_c N^2}{L} - \frac{l_c}{\mu_r} \\
 &= \frac{4 \times \pi \times 10^{-7} \times 0.417 \times 10^{-4} \times 91^2}{557 \times 10^{-6}} \\
 &\quad - \frac{7.2 \times 10^{-2}}{2300} \quad (\text{m}) = 0.748 \text{ mm},
 \end{aligned} \tag{26}$$

where  $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$  is the free-space permeability.

Here, we consider the fringing effect. The fundamental theory of the fringing effect is given in [5]. It is assumed that the ratio of the effective width of the fringing flux cross-sectional area  $w_f$  to the gap length is  $u = w_f/l_g = 1$ , and the ratio of the effective magnetic path length of the fringing flux to the gap length  $k = 2$ . The fringing flux factor  $F_f$  is

$$\begin{aligned}
 F_f &= 1 + \frac{2ul_g(C + F + 2ul_g)}{kCF} \\
 &= 1 + 2 \times 1 \times 0.748 \times 10^{-3} \\
 &\quad \times \frac{(7 + 6.8 + 2 \times 1 \times 0.748) \times 10^{-3}}{2 \times 7 \times 6.8 \times 10^{-6}} = 1.24.
 \end{aligned}$$

(27)

The number of turns including the fringing effect is

$$\begin{aligned}
 N' &= \sqrt{\frac{L(l_g/F_f + l_c/\mu_r)}{\mu_0 A_c}} \\
 &= \sqrt{557 \times 10^{-6}} \\
 &\quad \times \sqrt{\frac{0.748 \times 10^{-3}/1.24 + 7.2 \times 10^{-2}/2300}{4 \times \pi \times 10^{-7} \times 0.417 \times 10^{-4}}} \\
 &= 82.1 \text{ turns.}
 \end{aligned}$$

(28)

We pick an 82-turn winding for realizing the inductor. Therefore, the number of winding layers is

$$\begin{aligned}
 N_l &= \frac{d_o N'}{2D} \\
 &= \frac{0.98 \times 10^{-3} \times 82}{2 \times 12.2 \times 10^{-3}} = 3.29.
 \end{aligned}$$

(29)

We need about a 3-layer winding to realize the inductor. The length of the winding wire is

$$\begin{aligned}
 l_w &= N' l_T \\
 &= 82 \times 5.1 \times 10^{-2} = 4.18 \text{ m.}
 \end{aligned}$$

(30)

The low-frequency winding resistance, which is almost equal to the dc winding resistance, is given by

$$\begin{aligned}
 R_{wdc} &= \frac{\rho_w l_w}{A_w} \\
 &= \frac{1.72 \times 10^{-8} \times 4.64}{0.653 \times 10^{-6}} = 110 \text{ m}\Omega,
 \end{aligned}
 \tag{31}$$

where  $\rho_w = 1.72 \times 10^{-8} \Omega\text{m}$  is the resistivity of the copper at  $T = 20 \text{ }^\circ\text{C}$ . The dc winding power loss without the skin and proximity effect is

$$\begin{aligned}
 P_{wdc} &= \frac{R_{wdc} I_m^2}{2} \\
 &= \frac{0.11 \times 1.51^2}{2} = 0.125 \text{ W}.
 \end{aligned}
 \tag{32}$$

The skin depth of copper at  $f = 100 \text{ kHz}$  is

$$\begin{aligned}
 \delta_w &= \sqrt{\frac{\rho_w}{\pi \mu_0 f}} \\
 &= \sqrt{\frac{1.72 \times 10^{-8}}{\pi \times 4 \times \pi \times 10^{-7} \times 100 \times 10^3}} \text{ (m)} \\
 &= 0.209 \text{ mm}.
 \end{aligned}
 \tag{33}$$

We estimate the ac winding loss using Dowell's equation. The factor of Dowell's equation for a round wire, which is obtained in [4] and [6], is expressed as

$$\begin{aligned}
 A &= \left(\frac{\pi}{4}\right)^{\frac{3}{4}} \frac{d}{\delta_w} \sqrt{\frac{d}{d_o}} \\
 &= \left(\frac{\pi}{4}\right)^{\frac{3}{4}} \frac{0.912 \times 10^{-3}}{0.209 \times 10^{-3}} \sqrt{\frac{0.912 \times 10^{-3}}{0.98 \times 10^{-3}}} \\
 &= 3.51.
 \end{aligned}
 \tag{34}$$



By using  $A = 3.51$ , we obtain the winding ac-to-dc resistance ratio as

$$\begin{aligned}
 F_R &= A \left[ \frac{\sinh(2A) + \sin(2A)}{\cosh(2A) - \cos(2A)} \right] \\
 &\quad + \frac{2A(N_l^2 - 1)}{3} \left[ \frac{\sinh(2A) - \sin(2A)}{\cosh(2A) + \cos(2A)} \right] \\
 &= 3.51 \left[ \frac{\sinh(2 \times 3.51) + \sin(2 \times 3.51)}{\cosh(2 \times 3.51) - \cos(2 \times 3.51)} \right] \\
 &\quad + \frac{2 \times 3.51 \times (3^2 - 1)}{3} \\
 &\quad \times \left[ \frac{\sinh(2 \times 3.51) - \sin(2 \times 3.51)}{\cosh(2 \times 3.51) + \cos(2 \times 3.51)} \right] \\
 &= 22.2
 \end{aligned} \tag{35}$$

The high-frequency ac resistance is

$$\begin{aligned}
 R_{wac} &= F_R R_{wdc} \\
 &= 22.2 \times 0.11 = 2.44 \Omega.
 \end{aligned} \tag{36}$$

Therefore, the high-frequency ac winding power loss is

$$\begin{aligned}
 P_{wac} &= F_R P_{wdc} \\
 &= 22.2 \times 0.125 = 2.78 \text{ W}
 \end{aligned} \tag{37}$$

The core power loss per unit volume at  $f = 100 \text{ kHz}$  is obtained from the catalog [8] as  $P_v = 400 \times 10^3 \text{ W/m}^3$ . Therefore, the total core loss is

$$\begin{aligned}
 P_c &= P_v V_c = 400 \times 10^3 \times 3010 \times 10^{-9} \\
 &= 1.20 \text{ W}.
 \end{aligned} \tag{38}$$

The equivalent series resistance (ESR) representing the core loss is expressed as

$$\begin{aligned}
 R_c &= \frac{2P_c}{I_m^2} \\
 &= \frac{2 \times 1.2}{1.51^2} = 1.05 \Omega.
 \end{aligned} \tag{39}$$

Therefore, the total power loss in the inductor is

$$\begin{aligned} P_{cw} &= P_c + P_{wac} \\ &= 1.2 + 2.78 = 3.98 \text{ W.} \end{aligned} \quad (40)$$

The equivalent series resistance of the inductor is

$$\begin{aligned} R_{esr} &= R_{wac} + R_c \\ &= 2.44 + 1.05 = 3.49 \Omega. \end{aligned} \quad (41)$$

The quality factor of the inductor is

$$\begin{aligned} Q &= \frac{\omega L}{R_{esr}} \\ &= \frac{2 \times \pi \times 100 \times 10^3 \times 557 \times 10^{-6}}{3.49} \\ &= 100. \end{aligned} \quad (41a)$$

**Multi-Strand Winding.** In this section, the design of the resonant inductor with multiple-strand winding is carried out to avoid the skin and proximity effects. For this purpose, the diameter of a single wire strand should be

$$\begin{aligned} d_s < 2\delta_w &= \sqrt{\frac{\rho_w}{\pi\mu_0 f}} \\ &= \sqrt{\frac{1.724 \times 10^{-8}}{\pi \times 4 \times \pi \times 10^{-7} \times 100 \times 10^3}} \quad (\text{m}) \\ &= 0.418 \text{ mm.} \end{aligned} \quad (42)$$

The thickest wire less than  $2\delta_w$  is AWG 26 with the bare wire diameter  $d_s = 0.405 \text{ mm}$ , the insulated wire diameter  $\delta_{20} = 0.452 \text{ mm}$ , and the bare wire cross-sectional area  $A_{ws} = 0.128 \text{ mm}^2$ . The number of strands is

$$N_{strand} = \frac{A_w}{A_{ws}} = \frac{0.547}{0.128} = 4.2. \quad (43)$$

The number of strands  $N_{strand} = 4$  is selected. From (10), the number of turns is

$$\begin{aligned}
 N_s &= \frac{K_u W_a}{A_{wo}} = \frac{K_u W_a}{\frac{N_{strand} \pi d_{so}^2}{4}} \\
 &= \frac{0.4 \times 1.49 \times 10^{-4}}{4 \times \pi \times (0.452 \times 10^{-3})^2} = 92.7 .
 \end{aligned}
 \tag{44}$$

We pick  $N_s = 93$ . The inductance value is adjusted by tuning the gap length, which is

$$\begin{aligned}
 l_{gs} &= \frac{\mu_0 N^2 A_c}{L} - \frac{l_c}{\mu_r} \\
 &= \frac{4 \times \pi \times 10^{-7} \times 93^2 \times 0.417 \times 10^{-4}}{\frac{557 \times 10^{-6}}{7.2 \times 10^{-2}} - \frac{2300}{2300}} \text{ (m)} = 0.782 \text{ mm.}
 \end{aligned}
 \tag{45}$$

The fringing flux factor  $F_f$  is

$$\begin{aligned}
 F_{fs} &= 1 + \frac{2ul_{gs}(C + F + 2ul_{gs})}{kCF} \\
 &= 1 + \frac{2 \times 1 \times 0.782 \times 10^{-3}}{(7 + 6.8 + 2 \times 1 \times 0.782) \times 10^{-3}} \\
 &\quad \times \frac{2 \times 7 \times 6.8 \times 10^{-6}}{2 \times 7 \times 6.8 \times 10^{-6}} = 1.25.
 \end{aligned}
 \tag{46}$$

The number of turns including the fringing effect is

$$\begin{aligned}
 N_s' &= \sqrt{\frac{L(l_{gs}/F_{fs} + l_c/\mu_r)}{\mu_0 A_c}} \\
 &= \sqrt{557 \times 10^{-6}} \\
 &\quad \times \sqrt{\frac{0.782 \times 10^{-3}/1.25 + 7.2 \times 10^{-2}/2300}{4 \times \pi \times 10^{-7} \times 0.417 \times 10^{-4}}} \\
 &= 83.6 \text{ turns.}
 \end{aligned}
 \tag{47}$$

We pick  $N_s' = 84$ . The multi-strand wire length is

$$\begin{aligned} l_{ws} &= N_s' l_T \\ &= 84 \times 5.1 \times 10^{-2} = 4.28 \text{ m.} \end{aligned} \quad (48)$$

Therefore, the dc winding resistance is

$$\begin{aligned} R_{wdcs} &= \frac{\rho_w l_{ws}}{A_{wo}} = \frac{\rho_w l_{ws}}{\frac{N_{strand} \pi d_{so}^2}{4}} \\ &= \frac{1.72 \times 10^{-8} \times 4.28}{4 \times \pi \times (0.452 \times 10^{-3})^2} = 115 \text{ m}\Omega. \end{aligned} \quad (49)$$

Because the skin and proximity effects can be neglected, the winding loss is

$$\begin{aligned} P_{ws} &= \frac{R_{wdcs} I_m^2}{2} \\ &= \frac{0.115 \times 1.51^2}{2} = 0.131 \text{ W.} \end{aligned} \quad (50)$$

Therefore, the total power loss in the inductor is

$$\begin{aligned} P_{cw} &= P_c + P_{ws} \\ &= 1.2 + 0.131 = 1.33 \text{ W.} \end{aligned} \quad (51)$$

The equivalent series resistance of the inductor is

$$\begin{aligned} R_{esrs} &= R_{wdcs} + R_c \\ &= 0.115 + 1.05 = 1.16 \Omega. \end{aligned} \quad (52)$$

The quality factor of the inductor with multiple-strand winding is

$$\begin{aligned} Q &= \frac{\omega L}{R_{esrs}} \\ &= \frac{2 \times \pi \times 100 \times 10^3 \times 557 \times 10^{-6}}{1.16} \\ &= 302. \end{aligned} \quad (53)$$

Table 1 gives the design results for both  $\alpha = 0.005$  and  $\alpha = 0.0025$ . Since the example resonant inductor is designed for the high-frequency and high-power application, the current density restriction is a bottle-neck of the design. Additionally, it is shown that the core loss is much larger than the wire loss.

Table 1: Results for Resonant Inductor Designs for Multiple-Strand Winding.

Required $P_w$	Core	Material	$V_c$ (mm <sup>3</sup> )	Wire	$N_{strand}$	$N$	$P_w$ (W)	$P_c$ (W)	$J_m$ (A/mm <sup>2</sup> )
0.4	FEI25	BH1	1934	AWG26	2	83	0.402	0.77	<b>5.49</b>
0.2	FEE25W	BH1	3010	AWG26	4	84	0.115	1.20	2.77

### Conclusion

This paper has presented a novel core-selection criterion, taking into account the core loss. The proposed criterion indicates the core candidates, which satisfy the core-window-area restriction and the electromagnetic conditions with the guarantee of the permissible core-loss. It is confirmed from the design example that the designed inductor satisfies multiple restrictions simultaneously. The geometry coefficient  $K_g$  method is recommended for designing inductors for resonant power converters [9] and PWM dc-dc power converters [10], [11].

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